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Almost Contact Metric Submersions and Curvature Tensors

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ABSTRACT

It is known that L. Vanhecke, among others geometers, has studied curvature properties both on almost Hermitian and almost contact metric manifolds.

The purpose of this paper is to interrelate these properties within the theory of almost contact metric submersions. So, we examine the following problem: *Let* $f : M \longrightarrow B$ *be an almost contact metric submersion . Suppose that the total space is a* $C(\alpha)$*-manifold. What curvature properties do have the fibres or the base space*?

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