Complex Banach Spaces with Valdivia Dual Unit Ball [*]

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(Presented by Y. Benyamini)

ABSTRACT

We study the classes of complex Banach spaces with Valdivia dual unit ball. We give complex analogues of several theorems on real spaces. Further we study relationship of these complex Banach spaces with their real versions and that of real Banach spaces and their complexification. We also formulate several open problems.

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