A Note on the Stability of Linear Combinations of Algebraic Operators

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Abstract: The main purpose of this note is to characterize all the algebraic operators S and T having the same minimal polynomial and for which certain spectral properties of linear combinations of S and T do not depend on their coefficients.

Key words: Stability, invertibility, algebraic operator.

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