# A Note on the Class of Superreflexive
# Almost Transitive Banach Spaces

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*Abstract*: The class $\mathcal{J}$ of simultaneously almost transitive, uniformly convex and uniformly smooth Banach spaces is characterized in terms of convex-transitivity and the weak geometry of the norm.

*Key words*: almost transitive, convex-transitive, rough norm, superreflexive, weakly exposed points.

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