# Cartan Domains and Indefinite Euclidean Spaces

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*Abstract*: We prove that the complex hyperbolic space is the only Cartan domain which admits a Kähler immersion into the indefinite complex Euclidean space of finite index.

*Key words*: Kähler metrics; bounded domains; diastasis function; symmetric space; complex space form.

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