Trees and Point of Continuity Property in Banach Spaces [†]

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Abstract: We introduce the notion of topologically weakly null tree and, as a consequence, we get a characterization of the point of continuity property in general Banach spaces by extending to the general case some known results.

Key words: Point of continuity property, trees, boundedly complete sequences.

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