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Continuity of the Norm of Composition Operators

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Abstract: Let ϕ be an analytic self-map of the open unit disk $\mathbb{D}$ in the complex plane. Such a map induces a composition operator C_ϕ on weighted Banach spaces of holomorphic functions. We study when the norm of composition operators acting on weighted Banach spaces of analytic functions is continuous at a symbol.

Key words: norm of a composition operator, continuity, weighted Banach spaces of holomorphic functions.

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