

# On the decomposable semigroups. Applications

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## Abstract

In this paper we study some properties of decomposable semigroups and their associated ideals. We give an efficient method to determine the decomposition of this kind of semigroups which improves the computation of some objects related with them. In particular, we apply these improvements to some semigroups studied in Algebraic Statistics. We also prove a combinatorial characterization of decomposable semigroups.

## References

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