

# Formulario

## Trigonometría esférica

- Área:  $S = r^2\epsilon$  (exceso esférico en radianes)
- $\frac{\operatorname{sen} a}{\operatorname{sen} A} = \frac{\operatorname{sen} b}{\operatorname{sen} B}$ ,  $\cos a = \cos b \cos c + \sin b \sin c \cos A$ .
- $\cot a \operatorname{sen} b = \cos b \cos C + \sin C \cot A$ ,  $\cos A = -\cos B \cos C + \sin B \sin C \cos a$ .
- $\frac{\operatorname{sen} \frac{A+B}{2}}{\cos \frac{C}{2}} = \frac{\cos \frac{a-b}{2}}{\cos \frac{c}{2}}$ ,  $\frac{\operatorname{sen} \frac{A-B}{2}}{\cos \frac{C}{2}} = \frac{\operatorname{sen} \frac{a-b}{2}}{\operatorname{sen} \frac{c}{2}}$ ,  $\frac{\cos \frac{A+B}{2}}{\operatorname{sen} \frac{C}{2}} = \frac{\cos \frac{a+b}{2}}{\cos \frac{c}{2}}$ ,  $\frac{\cos \frac{A-B}{2}}{\operatorname{sen} \frac{C}{2}} = \frac{\operatorname{sen} \frac{a+b}{2}}{\operatorname{sen} \frac{c}{2}}$ .
- $\frac{\tan \frac{A+B}{2}}{\cot \frac{C}{2}} = \frac{\cos \frac{a-b}{2}}{\cos \frac{a+b}{2}}$ ,  $\frac{\tan \frac{A-B}{2}}{\cot \frac{C}{2}} = \frac{\operatorname{sen} \frac{a-b}{2}}{\operatorname{sen} \frac{a+b}{2}}$ ,  $\frac{\tan \frac{a+b}{2}}{\tan \frac{c}{2}} = \frac{\cos \frac{A-B}{2}}{\cos \frac{A+B}{2}}$ ,  $\frac{\tan \frac{a-b}{2}}{\tan \frac{c}{2}} = \frac{\operatorname{sen} \frac{A-B}{2}}{\operatorname{sen} \frac{A+B}{2}}$ .

## Resolución de ecuaciones

- Bisección:  $c = (b+a)/2$ ,  $E_n = \frac{b-a}{2^n}$ .
- Newton-Raphson:  $x_{n+1} = x_n - f(x_n)/f'(x_n)$ ,  $E_{n+1} = \frac{f''(\xi)}{2f'(x_n)}E_n^2$ . Secante:  $x_{n+2} = \frac{f(x_{n+1})x_n - f(x_n)x_{n+1}}{f(x_{n+1}) - f(x_n)}$
- Punto fijo:  $x_n = F(x_{n-1})$ ,  $E_{n+1} \leq K^n \frac{|x_1 - x_0|}{1-K}$
- Jacobi:  $Dx_{k+1} = -(L+U)x_k + b$ . Gauss-Seidel:  $(D+L)x_{k+1} = -Ux_k + b$
- Sistemas no lineales (Newton):  $\mathbf{J}(\mathbf{x}_n)(\mathbf{x}_{n+1} - \mathbf{x}_n) = -F(\mathbf{x}_n)$

## Interpolación e integración

- Error de interpolación:  $f(x) - P_n(x) = \frac{f^{(n+1)}}{(n+1)!}(x-x_0)(x-x_1)\dots(x-x_n)$
- Lagrange:  $L_i(x) = \frac{\prod_{j \neq i}(x-x_j)}{\prod_{j \neq i}(x_i-x_j)}$
- Diferencias divididas:  $f[x_k] = f(x_k)$ ,  $f[x_i, x_{i+1}, \dots, x_j] = \frac{f[x_{i+1}, x_{i+2}, \dots, x_j] - f[x_i, x_{i+1}, \dots, x_{j-1}]}{x_j - x_i}$   
 $p(x) = f[x_0] + f[x_0, x_1](x-x_0) + f[x_0, x_1, x_2](x-x_0)(x-x_1) + \dots + f[x_0, x_1, \dots, x_n](x-x_0)(x-x_1)\dots(x-x_{n-1})$ .
- Trapecio:  $\int_a^b f(x) dx \approx \frac{h}{2}(f(a) + f(b))$ . Error  $-\frac{(b-a)^3}{12}f''(\xi)$ .
- Simpson:  $\int_a^b f(x) dx \approx \frac{h}{3}(f(a) + 4f(x_1) + f(b))$ . Error  $-\frac{(b-a)^5}{720}f^{(4)}(\xi)$ .
- Trapecio compuesto:  $\int_a^b f(x) dx \approx \frac{h}{2}(f(x_0) + 2f(x_1) + \dots + 2f(x_{n-1}) + f(x_n))$

## Ecuaciones diferenciales

- Ecuación lineal:  $x(t) = x(t_0)\exp(A(t)) + \exp(A(t)) \int_{t_0}^t b(s)\exp(-A(s)) ds$
- Método de Euler:  $x_{k+1} = x_k + hf(t_k, x_k)$
- Método de Euler modificado:  $x_{k+1} = x_k + \frac{h}{2}\left(f(t_k, x_k) + f(t_k + h, x_k + hf(t_k, x_k))\right)$